# Key

## Chi-Square

How do you know if your data is the result of random chance or environmental factors?

## Why?

Biologists and other scientists use relationships they have discovered in the lab to predict events that might happen under more real-life circumstances. At some point those predictions are either supported or not by real data. It would be nice if the two sets of data matched exactly, but more often than not they don't. This could be attributed to random fluctuations in the variables, or it could be due to a factor that the scientists overlooked. How does the scientist know? There are many statistical calculations that help answer this question. One that is commonly used by biologists is **Chi-Square**.

## Model 1 – Calculating Chi-Square ( $\chi^2$ )

Hypoth	esis: There is a	ın equal chanc	e of flipping	heads or tai	ls on a coin.	
Coin A						
	Observed data (0)	Expected (e)	(o – e)	$(o - e)^2$	$\frac{(o-e)^2}{e}$	$\chi^2 = \Sigma (\underline{o-e})^2$
Heads	108	100	8	64	.64	
Tails	92	100	-8	64	.64	
Total	200	200				$\chi^2 = 1.28$

Coin E	3					
	Observed data (0)	Expected (e)	(o – e)	$(o - e)^2$	$\frac{(o-e)^2}{e}$	$\chi^2 = \Sigma (o - e)^2$
Heads	120	100	20	400	4	
Tails	80	100	-20	400	4	
Total	200	200				x2=8

1. What is the hypothesis that has been tested in Model 1?
There is an equal charge of thipping heads or tails

2. Describe in one or two complete sentences the experiment being performed in Model 1.

A coin is being flipped to heads or tails

3. How many flips of the coin will be conducted in each trial for the experiment in Model 1?

- 4. How many of the 200 flips would you expect to be heads and how many would you expect to be tails? Fill in the expected (e) column of Model 1 for both coin A and coin B.
- 5. Assume the experiment for coin A resulted in 108 heads and 92 tails. Fill in the data table for coin A under observed (o).
- 6. The experiment was repeated with a different coin. coin B resulted in 120 heads and 80 tails. Fill in the data table for coin B under observed (o).
- 7. If you were told that one of the coins used in the experiments in Model 1 was a "trick" coin, which coin would you predict was rigged? Explain your reasoning.

  Coin b. It was further from expected walks.

#### Read This!

The experiments in Model 1 did not give the expected outcome, so the question becomes: Is this due to random chance, or does the coin being flipped favor heads for some reason? The statistical calculation of **chi-square** ( $\chi^2$ ) will help determine if there is a significant difference between the expected outcome and the observed outcome. In statistics a "significant" difference means there is less than 5% chance that the variation in the data is due to random events. Therefore, the variation is most likely due to an environmental factor.

- 8. What symbol represents chi-square? 2
- 9. Use the equations in Model 1 to complete the calculations of  $\chi^2$  for coin A and coin B.



- 10. Circle the correct phrase to complete the sentence.

  A larger chi-square value means the observed data is (very different from/very similar to) the expected data.
- 11. One hundred heterozygous (Bb) males mate with one hundred heterozygous (Bb) females.
  - a. Draw a Punnett square to show the possible genotypes of the offspring from each pairing.



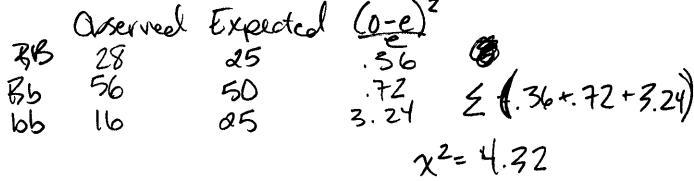
b. Predict the number of offspring from the 100 mating pairs that will be each genotype.

$$BB = 25 Bb = 50 bb = 25$$

$$(100 \times .25) (100 \times .5) (100 \times .25) POGIL^{TM} Activities for AP* Biology$$

$$(100 \times \frac{1}{4}) (100 \times \frac{1}{4}) (100 \times \frac{1}{4})$$

c. The observed outcome from this experiment is 28 BB offspring, 56 Bb offspring and 16 bb offspring. Use a table similar to that in Model 1 to calculate chi-square for this experiment.



d. In your opinion, is the observed data significantly different from the expected data in this mating experiment? Justify your answer.

Varies -> needs statistical awailysis to

#### Read This!

To determine if the chi-square value is large enough to be "significant," researchers need one more thing—degrees of freedom. If an experiment has five possible equivalent outcomes, then in reality there is one result and four additional possible results, making a total of five. The degrees of freedom are always calculated as the number of possible outcomes minus one.

- 12. Consider the coin flip experiments in Model 1 where you could get heads or tails.
  - a. How many outcomes were possible in the coin flip experiments?
  - b. How many degrees of freedom were there in the coin flip experiments?
- 13. Consider the mating organisms in Question 11.
  - a. How many genotype outcomes were possible in that experiment? 3
  - a. How many degrees of freedom were there in that experiment? 2

# Model $2 - \chi^2$ Analysis

Degrees of Freedom	χ² Values										
1	0.004	0.02	0.06	0.15	0.46	1.07	1.64	2.71	3.84	6.64	10.83
2	0.10	0.21	0.45	0.71	1.39	2.41	3.22	4.60	5.99	9.21	13.82
3	0.35	0.58	1.01	1.42	2.37	3.66	4.64	6.25	7.82	11.34	16.27
4	0.71	1.06	1.65	2.20	3.36	4.88	5.99	7.78	9.49	13.28	18.47
5	1.14	1.61	2.34	3.00	4.35	6.06	7.29	9.24	11.07	15.09	20.52
P Value =	0.95	0.9	0.8	0.7	0.5	0.3	0.2	0.1	0.05	0.01	0.001
% probability	Not Significant Significa							cant			

14.	The table in Model 2 has	three types of values—χ <sup>2</sup>	, degrees of freedom,	and P values or
	probabilities.			

a. Which of these are along the bottom of the table?  P values (probabilities)
b. Which of these are along the side of the table?  Degrees & Arcedon
c. What chi-square value is needed to have a P value of 0.5 in an experiment with two degrees of freedom?  1.37
15. The table in Model 2 is a reference table used by scientists to interpret the calculated chi-square value for their experiment. It converts the chi-square value into a probability that the differences in the data are only due to chance.
a. Which P Values in the table indicate that the difference between the expected and observed data was likely due to chance?  95-1 are Not Significant + : only due  b. Which P Values in the table indicate that the difference between the expected and observed data was likely due to an environmental factor?  O Values 1853 than . 05 are significant - the
p values less than .05 are significant - the is probably another explanation for the aitherences by dos. + expected  16. What does a P value of 0.7 mean in terms of percent chance that the data sets are different only
There is a 70% chance that the Washability in data is only due to Chance.
by chance? There is a 70% chance that the Variability in data is only due to Chance. Not significant different OGIL besture Bology observed and expleted data
•

17. As the chi-square values get larger, is the data more likely to be significant or not significant?
data is different than expected values
18. When an experiment has more degrees of freedom, is a larger chi-square needed for a significant
outcome, or is a smaller chi-square needed for a significant outcome? $\chi^2$ to get
sure p value
19. Which row of $\chi^2$ values in Model 2 should be used for the coin flip experiments?
19. Which row of χ² values in Model 2 should be used for the coin flip experiments?
·
20. Find the P values for each coin experiment in Model 1 using the $\chi^2$ values in Model 2.
<i>Note:</i> If the $\chi^2$ value falls between two points on the chart, give a range of P values.
a. Coin A = between ·2 + ·3
b. Coin B = between . 01 + . 001
21. Consider your answers in Question 20,
<ul> <li>a. Which coin produced a nonsignificant χ² value, indicating that the outcome was not statistically different from what was expected?</li> <li>Coin A</li> </ul>
<ul> <li>b. Which coin produced a significant χ² value, indicating that the outcome was statistically different from what was expected and therefore due to an environmental factor?</li> </ul>
c. With your group propose an explanation for why the results of either coin were statistically significant. Coin was weighted or althoughted we pripped heads more often
22. Does the mating experiment from Question 11 indicate that an environmental factor was affecting the outcome? Justify your answer using information from Model 2.
~2 127 2 150
1 1/2 21 1 Axt SIChia cantl
praid 610 .2 4 .1, out, 100 contents
prature 6/w .2 + .1, Not significantly Lightent than expected outcome
111.3

23. A researcher is investigating a flowering plant. The purple flower allele, P, is dominant to the white flower allele, p. A cross was performed between a purple-flowered plant and a whiteflowered plant. The 206 seeds that were produced from the cross matured into 124 purpleflowered plants and 82 white-flowered plants. Construct a table similar to those in Model 1 to calculate chi-square for the null hypothesis that the purple-flowered parent plant was heterozygous,

P=pur pp=w	do nite	Pp ×	66		
` ` ` ` ` ` ` ` ` ` ` ` ` ` ` ` ` ` ` `		P	( <del>-</del> )		purplo
	(	P) Pp 1 expecte	PP (0-e)2	50%	white
	observed	l expecte	d 6-61		
Pordo (Pe)	124	103	4.28		
Porpo (Pp) White (pp)	82	103	4.28		
	206	206	$\chi^2 = 85$	56	

Of =

- Observed data is significantly different than expected.

- Our hypothesis is rejected, the differences between the expected values of the doserved data is too targe to be the doserved data is too targe to be we to random chance alone

### **Extension Questions**

- 24. You have performed a dihybrid cross of plants and got the following data: 206 purple tall, 65 white tall, 83 purple short, 30 white short.
  - a. Using your knowledge of genetics, determine the expected outcome for this experiment.

Port x Port - 9:3:5:1 Total plants

Purple tall - The expected 216

purple short 3 72

white tall
b. What are the degrees of freedom in this experiment?

c. Calculate chi-square for your experimental data below.

	Observed data (0)	Expected (e)	(o - e)	$(o-e)^2$	$\frac{(o-e)^2}{e}$
Purple and tall	206	216	-10	100	.463
Purple and short	83	72	11	121	1.681
White and tall	65	72	- 7	49	.681
White and short	30	24	6	36	1.5

 $\chi^2 = 4.325$ 

d. Does your collected data differ significantly from the expected values? Explain.

observed & expected is not significant so we do not reject our hypothesis (our results stastically support our hypothesis)

(Differences blue observed & expected data a small enough to be square due to random chance)